

## CLUSTER DIMENSION OF A NETWORK

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### Abstract

We define the *Cluster Dimension* of a network is the minimum cardinality of a subset  $S$  of the set of nodes having the property that for any two distinct nodes  $x$  and  $y$ , there exist the node  $s_1, s_2$  (need not be distinct) in  $S$  such that  $|d(x, s_1) - d(y, s_1)| \geq 1$  and  $d(x, s_2) < d(x, s)$  for all  $s \in S - \{s_2\}$ . In this paper, we obtain sufficient conditions for a graph of cluster dimension  $n$  and a tight upper bound for the number of nodes of a network with prescribed dimension in terms of diameter. Also give an algorithm to determine cluster basis and dimensions of a given graph to show the *NP* completeness.

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