International J. of Math. Sci. & Engg. Appls. (IJMSEA) ISSN 0973-9424, Vol. 6 No. IV (July, 2012), pp. 211-221

COMPLEMENTARY EDGE SEMITOTAL-POINT DOMINATION IN GRAPHS

B. BASAVANAGOUD, S. M. HOSAMANI AND S. H. MALGHAN

Department of Mathematics, Karnatak University, Dharwad -580 003, India

Abstract

For any graph G = (V, E), the semitotal-point graph $T_2(G) = H$ is the graph whose point set is the union of vertices and edges of G, in which two vertices are adjacent if and only if they are adjacent vertices of G or one is a vertex and the other is an edge of G incident with it. Let F be a minimum edge dominating set of G. If E - F contains an edge dominating set F', then F' is called a complementary edge dominating set of G with respect to F. The complementary edge domination number $\gamma_e^{-1}(G)$ of G is the minimum number of edges in a complementary edge dominating set of G. A complementary edge dominating set of a graph H is called a complementary edge semitotal-point dominating set of G. A complementary edge semitotal-point domination number $\gamma_{etp}^{-1}(G)$ of G is the minimum cardinality of a complementary edge semitotal-point dominating set of G. In this paper, many bounds on $\gamma_{etp}^{-1}(G)$ are obtained in terms of elements of G but not the elements of H. In addition, we establish the relationship of this concept with other domination parameters. Also, Nordhaus-Gaddum type results are obtained.

Key Words : Domination number, Edge domination number, Complementary edge domination number.

2000 AMS Subject Classification : 05C69.

© http://www.ascent-journals.com