

IDEMPOTENTS IN THE NUCLEUS OF AN ASSOSYMMETRIC RING

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Abstract

In this paper we show that in an assosymmetric ring R , an idempotent $e \neq 0$ is in the nucleus N . The assosymmetric ring was introduced by E. Kleinfeld in [3] is a nonassociative ring in which the associator $(x; y; z) = (xy)z - x(yz)$ has the property $(x; y; z) = (P(x); P(y); P(z))$ for each permutation P of $x; y; z$ in R . These rings are neither exible nor power associative, not commutative and not semiprime [1]. E. Kleinfeld in [3] has shown that the associator and the commutator are in the nucleus of an assosymmetric ring. By using these properties, first we show that in an assosymmetric ring R , an idempotent $e \neq 0$ is in the nucleus N . We also prove that if R is prime, then e is the identity element of R . We give an example of an assosymmetric ring which does not have Pierce decomposition with respect to the idempotent e . A ring is said to be prime if for any ideals A and B of R , $AB = (0)$ implies either $A = (0)$ or $B = (0)$. A ring is simple if for any ideal A of R either $A = (0)$ or $A = R$. A ring R is said to have Pierce decomposition relative to the idempotent $e \in R$, if R can be decomposed into the direct sum of Z -modules R_{ij} ($i, j = 0; 1$) where $R_{ij} = \{x \in R : ex = ix \text{ and } xe = jx\}$. The commutator $[x; y]$ is defined by $xy - yx$.

Key Words and Phrases : Assosymmetric ring, Prime ring, Nucleus, Idempotent.

2000 Mathematics Subject Classification: 17A01.

Ascent Publication House: [http:// www.ascent-journals.com](http://www.ascent-journals.com)